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**та математичні методи**

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## EVALUATION OF FIRE RESISTANCE OF FIRE PROTECTED STEEL STRUCTURES BY CALCULATION AND EXPERIMENTAL METHOD

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**Abstract:** Based on the developed geometric, physical, computer and finite element model, the fire resistance of fire-resistant steel structures was evaluated by calculation and experimental method. The adequacy of the developed computational-experimental method for assessing the fire resistance of fire-resistant steel structures in assessing the fire resistance of a fire-resistant I-beam steel column was verified. The results of tests for fire resistance of steel columns with fire-retardant coating at standard temperature of the fire without the load applied to them (temperature in the furnace, temperature in certain places on the surface of fire-retardant steel columns, the behavior of the investigated fire-retardant coating). The analysis of tests on fire resistance of fire-resistant steel columns exposed to fire at standard temperature (temperature in the furnace, temperature in places of measurement of temperature on a surface of columns, behavior of a fire-retardant covering) is carried out. A computer model of the «steel column – reactive flame retardant coating» system has been built for numerical simulation of non-stationary heating of such a system. Simulation of non-stationary heating of the system «steel column – fire-retardant coating» in the software package FRIEND with the specified parameters (geometric model, thermal effects, initial and boundary conditions, properties of system materials). The reliability of the results of numerical modeling with real experimental data on the duration of fire exposure at the standard temperature of the fire to reach the critical temperature of steel. Based on the comparison of experimental results and numerical simulations, a conclusion is made about the adequacy of the developed model to the real processes that occur when heating fire-retardant steel columns without applying a load under fire conditions at standard fire temperature. The efficiency of the proposed calculation and experimental method for assessing the fire resistance of fire-resistant steel structures has been confirmed.

**Keywords:** fire resistance, method of fire resistance assessment, fire protection, fire protection ability, fire protective coatings, steel structures.

## ОЦІНЮВАННЯ ВОГНЕСТІЙКОСТІ ВОГНЕЗАХИЩЕНИХ СТАЛЕВИХ КОНСТРУКЦІЙ РОЗРАХУНКОВО-ЕКСПЕРИМЕНТАЛЬНИМ МЕТОДОМ

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**Анотація:** На основі розроблених геометричної, фізичної, комп'ютерної та скінченно-елементної моделі здійснено оцінювання вогнестійкості вогнезахисених сталевих конструкцій розрахунково-експериментальним методом. Проведено перевірку адекватності розробленого розрахунково-експериментального методу оцінювання вогнестійкості вогнезахисених сталевих конструкцій при оцінюванні вогнестійкості вогнезахисеної двотаврової сталевій колони. Представлено результати випробувань на вогнестійкість сталевих колон з вогнезахисним покриттям при стандартному температурному режимові пожежі без



прикладеного до них навантаження (температура в печі, температура у визначених місцях на поверхні вогнезахисних сталевих колон, поведінка досліджуваного вогнезахисного покриття). Проведено аналіз випробувань на вогнестійкість вогнезахисних сталевих колон, що піддавалися впливу пожежі за стандартним температурним режимом (температура в печі, температура у місцях вимірювання температури на поверхні колон, поведінка вогнезахисного покриття). Побудовано комп'ютерну модель системи «сталеві колон – реактивне вогнезахисне покриття» для чисельного моделювання нестационарного прогріву такої системи. Проведено моделювання нестационарного прогріву системи «сталеві колон – вогнезахисне покриття» в програмному комплексі FRIEND з заданими параметрами (геометрична модель, теплові впливи, початкові та граничні умови, властивості матеріалів системи). Проведено оцінку достовірності результатів чисельного моделювання з реальними експериментальними даними щодо тривалості вогневого впливу за стандартним температурним режимом пожежі до досягнення критичної температури сталі. На основі порівняння результатів експерименту та чисельного моделювання зроблено висновок про адекватність розробленої моделі реальним процесам, що відбуваються при нагріванні вогнезахисних сталевих колон без прикладення навантаження в умовах вогневого впливу за стандартного температурного режиму пожежі. Підтверджена працездатність запропонованого розрахунково-експериментального методу оцінювання вогнестійкості вогнезахисних сталевих конструкцій.

**Ключові слова:** вогнестійкість, метод оцінювання вогнестійкості, вогнезахист, вогнезахисна здатність, вогнезахисні покриття, сталеві конструкції.



## 1 INTRODUCTION

Despite technical advances in construction and fire-fighting technologies, the latter has not become less dangerous. Fires claim thousands of lives and cause billions in damage. About 51% of all fires in the world occur in buildings and structures and transport. At the same time, 90% of all fire victims die on the premises.

These factors create a need to protect people from the impact of the identified threats. One of the most dangerous factors is fires in buildings and structures. Ensuring the safety of people and property must be performed taking into account all stages of the life cycle of facilities, such as scientific support and monitoring, design, construction, operation, as well as to exclude fires. Preventing the occurrence of fire allows technical means and organizational measures, in which the probability of occurrence and development of fire does not exceed the standard allowable value. The condition for reducing the irreversible consequences of fires at various facilities is the preservation of the bearing capacity of buildings, structures of technological structures and communications.

These stability requirements are provided by a set of measures provided for both production technology and the use of effective fire-retardant coatings for fire protection of building structures.

Therefore, in the context of globalization and increasing threats to humans, the first place is played by maintaining the resilience of buildings and structures in the event of fires and other natural disasters, as well as preserving their functional purpose after such impacts.

## 2 ANALYSIS OF LITERATURE DATA AND PROBLEM STATEMENT

Many well-known scientists have dealt with the issues of fire resistance assessment of fire-resistant steel structures. In [1], the authors developed two models of steel beams using ANSYS and OpenSEES programs, which take into account the constant mechanical load and the influence of fire temperature but do not take into account the presence of fire protection systems and their impact on modelling accuracy. The authors in [2] propose to use in the calculation of the temperature of fire-resistant steel structures in case of a fire a constant value of the thermal conductivity of the reactive fire-retardant coating, as it does not affect the accuracy of the calculations. However, as is known, the greatest accuracy of calculations is at the value of the thermal conductivity of the fire-retardant coating, which depends on the temperature. In [3] the results of the test for fire resistance of unprotected steel beams in comparison with simple and improved calculation methods given in EN 1993-1-2 are presented. The results showed the difference between the experimental and calculated temperature values obtained by FEM analysis. [4] presents a method for assessing the fire resistance of fire-resistant reactive fire-retardant coatings of steel structures. The method can be used to predict the behaviour of fire-retardant steel structures in different conditions (change in the coefficient of a cross-section of steel, coating thickness and type of fire exposure). However, there are no reliable data on the versatility of the method, including for passive fire-retardant coatings and the influence of climatic factors. In [5] experimental and calculated data on the determination of the temperature of steel plates with a fire-retardant covering in the conditions of fire influence on a standard fire have resulted. The authors analyze the possibility of using samples of reduced size and shape other than the size and shape of standardized samples of steel structures to assess the fire resistance of fire-resistant steel structures. In [6] we consider the results of experimental tests of steel plates of different sizes with water-based flame retardant coating, aimed at studying the thermal properties and the ratio of temperature and thickness of the coating in tests of steel plates of different thicknesses at standard temperature or slow-moving fire. However, the issues of the influence

of fire temperature regimes on the accuracy of fire resistance assessment of fire-resistant steel structures have not been fully investigated.

The conducted analysis allows to state the tendency to spread the application of the calculation-experimental method for estimating the limits of fire resistance of fire-resistant steel building structures and fire-retardant ability of coatings for such structures. This method allows taking into account the values of thermophysical characteristics of fire-retardant coatings not only as constant values but also as a function of temperature. This allows to increase the accuracy of the method and take into account the processes of heat transfer in the fire-resistant steel structure under the influence of different temperature regimes of fire.

Thus, the unsolved part of the problem is the lack of effective methods for assessing the fire resistance of fire-resistant steel building structures with scientifically sound parameters of fire protection systems in the form of both reactive and passive fire-retardant coatings. Solving this problem will increase the accuracy of estimating fire-resistant steel structures with sufficient accuracy for engineering calculations using the results of fire resistance tests, which are fully correlated with the results of numerical simulations in modern software packages.

### 3 THE PURPOSE AND OBJECTIVES OF THE STUDY

The work aims to assess the fire resistance of fire-resistant steel structures using the developed calculation and experimental method.

To achieve this goal needed to solve the following tasks:

- to analyze the results of tests for fire resistance of 2 fire-retardant steel columns;
- to build a physical, geometric, computer model of non-stationary heating of a fire-retardant steel column, in which to take into account and build:
  - the geometry of the object under study;
  - finite element model;
  - thermal effects on the structure;
- choose the calculation algorithm for processing the obtained experimental data.

### 4 ANALYSIS OF FIRE RESISTANCE TEST RESULTS

The test was subjected to 2 steel columns of I-beam section HEB 200 (thickness 6.1 mm), height 2 m. The columns were treated with flame retardant “Amotherm Steel Wb” after the pre-application of soil GF-021. Three thermocouples were placed on each sample according to [7], as shown in Fig. 1.

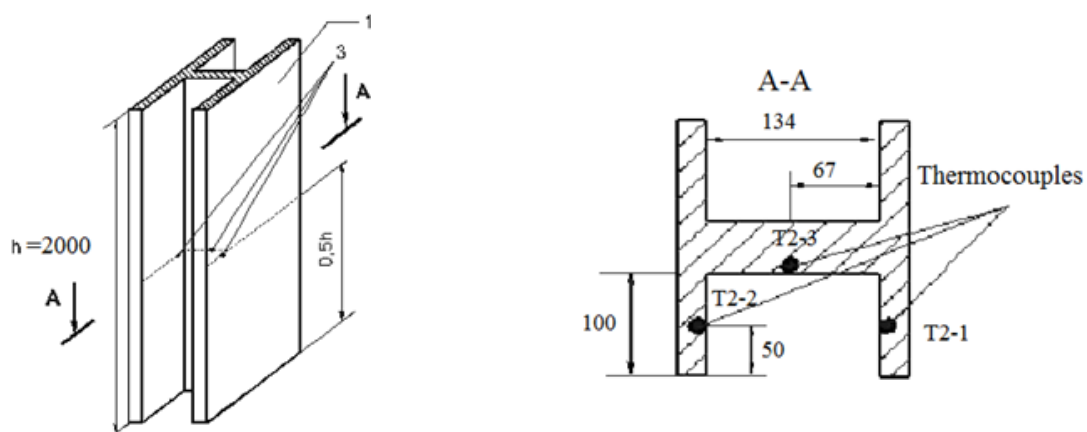
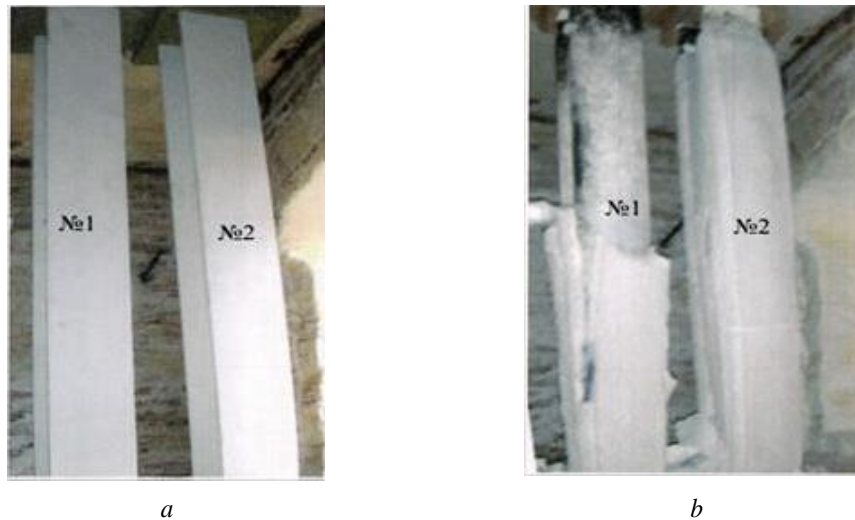


Fig. 1. Diagram of the location of thermocouples on samples of columns that are tested without load

The flame retardant was applied by mechanization and manually. The average coating thickness was 2.927 mm. The experiment was performed at an air temperature of 27°C, relative humidity of 54%. The average thickness of the coating of flame retardant “Amotherm Steel Wb” was (dry state without soil) 2.928 mm on the sample № 1 and 2.925 mm – on the sample № 2. Fig. 2 shows the types of samples in the furnace before (a) and after (b) the tests.



**Fig. 2.** Types of samples in the furnace before (a) and after (b) the tests

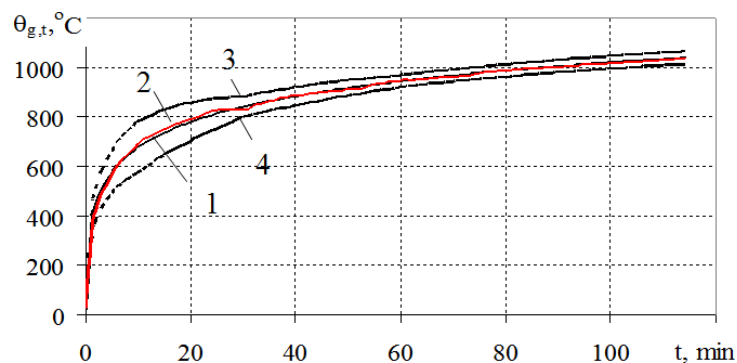
A special test furnace and metrological calibrated measuring equipment were used for the tests.

The temperature of the fire was determined by the formula:

$$\Theta_g = 20 + 345 \lg(8t + 1), \quad (1)$$

where  $\Theta_g$  – the temperature of the gas environment in the fire compartment, °C;  $t$  – time, min.

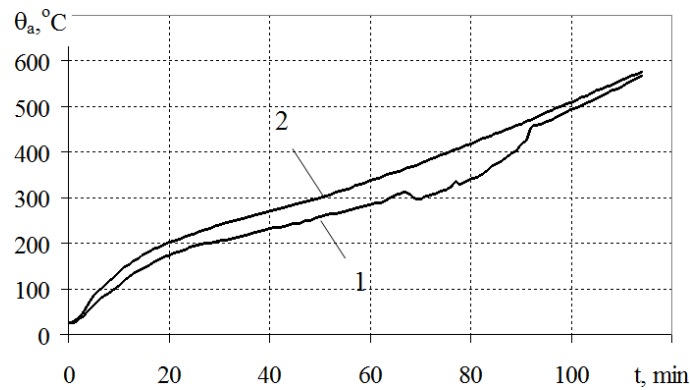
The temperature in the furnace was reproduced according to the standard temperature of the fire (Fig. 3).



**Fig. 3.** Dependence of temperature in the furnace on the duration of fire influence: 1 – a curve of a standard temperature mode, 2 – a real curve of change of temperature in the furnace; 3 – the maximum values of temperature in the furnace are admissible at tests; 4 – the minimum values of temperature in the furnace are admissible at tests

The volume swelling coefficient of the Amotherm Steel Web coating was 38.3 cm<sup>3</sup>/g (conditional linear swelling factor 47.9).

The dependence of the average temperatures of the samples of steel columns with the investigated fire-retardant coating on the time of fire exposure to the standard temperature of the fire is shown in Fig. 4.



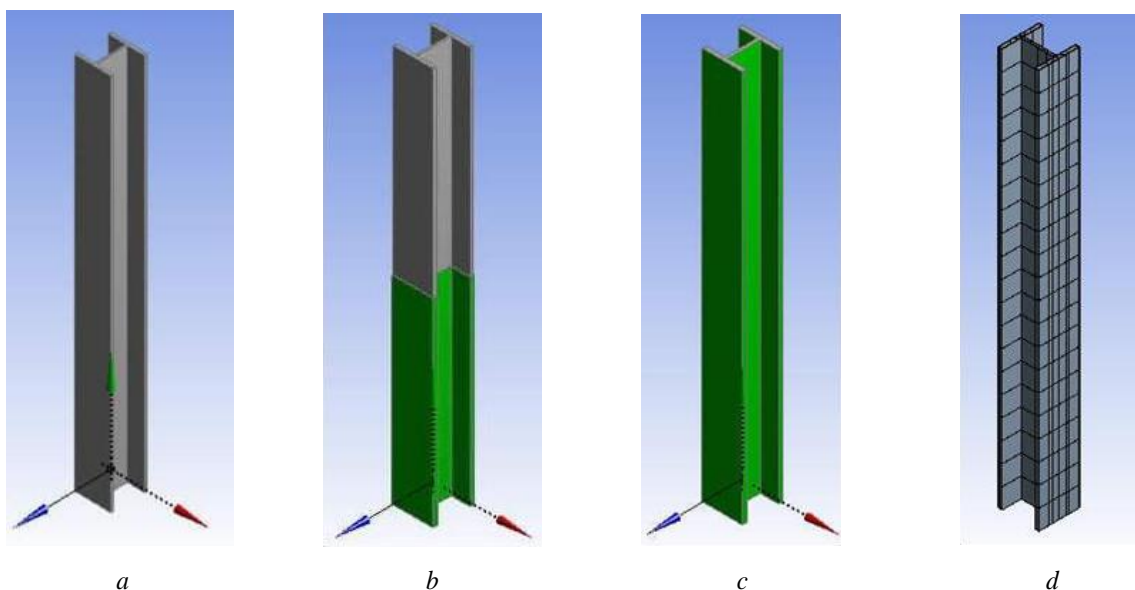
**Fig. 4.** Dependence of average temperatures of samples of fire-retardant steel columns on the time of fire exposure according to the standard temperature of the fire: 1 – sample column F 1; 2 – sample column F 2

As shown in Fig. 4 temperature dependences were compared with the results of computer simulation of non-stationary heating of a fire-retardant steel column, performed using FRIEND software.

These temperatures were compared with the results of computer simulations of non-stationary heating of a fire-retardant steel column, performed using FRIEND software. To compare the simulation results with the experimental determination of the temperature of the steel column in certain places under fire conditions according to the standard temperature of the fire, we took the values of the column sample temperature № 2 (Fig. 4, curve 2), which warmed up the most.

## 5 CONSTRUCTION OF MODELS OF NON-STATIONARY HEATING OF FIRE-RETARDANT STEEL COLUMN

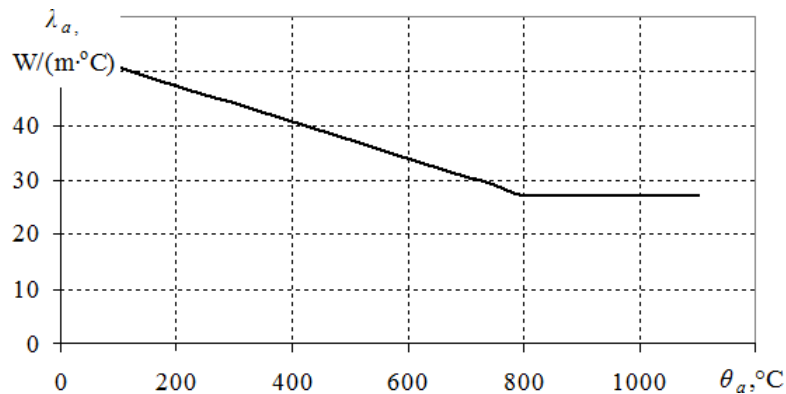
The computer model of the thermal state of the investigated fire-retardant column was built on the basis that the column is heated in the furnace on four sides equally. Therefore, each surface of the column is considered as a two-layer system consisting of a layer of steel and a layer of fire-retardant coating of appropriate thickness. This model allows the calculation of the temperature distribution at all spatial points of the layers over time and, in particular, at the locations of thermocouples not only by the standard temperature of the fire but also by other alternative fire modes (Fig. 5).



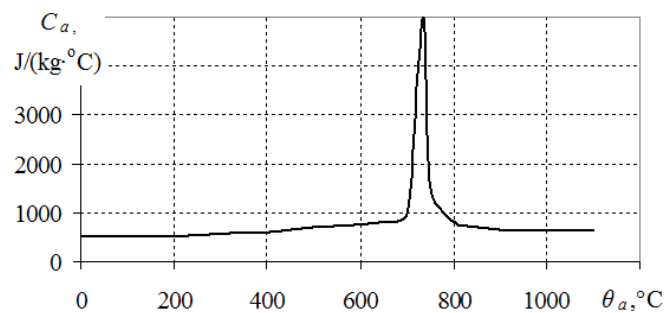
**Fig. 5.** Construction of geometric (a, b, c) and finite element model (d) of fire-retardant steel column



Thermal conductivity  $\lambda_a$  and the specific heat of steel  $c_a$  asked according to [9] and Fig. 8, 9.



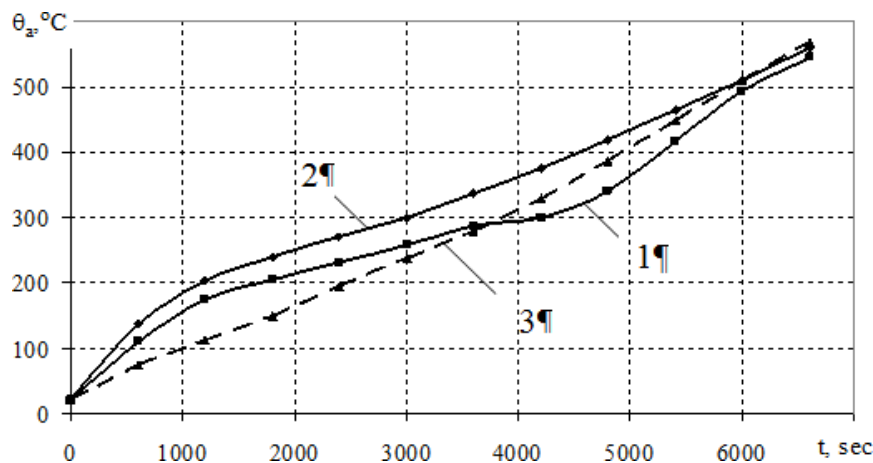
**Fig. 8.** Dependence of the thermal conductivity of steel on temperature



**Fig. 9.** Dependence of heat capacity of steel on temperature

The number of nodes of the numerical model was 15 nodes (10 nodes for steel structure and 5 nodes for fire protection coating) in spatial coordinates with a time step of 60 sec.

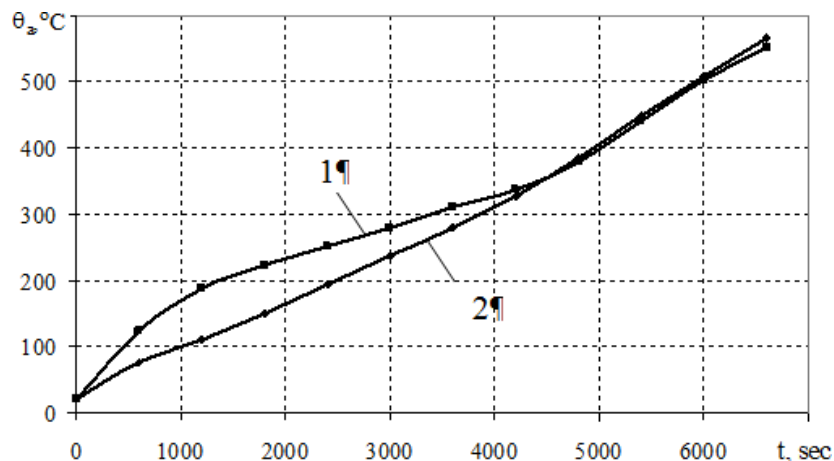
As a result of numerical modelling by solving direct problems of thermal conductivity, the calculated values of heating of a fire-retardant steel column were obtained, which are shown in Fig. 10.



**Fig. 10.** Dependence of temperature of fire-protected steel columns on time of fire influence on a standard temperature mode of a fire: 1 – the experimental curve of heating of column F 1; 2 – the experimental heating curve of column F 2; 3 – curve calculated as a result of numerical simulation

As can be seen from Fig. 10, calculated as a result of numerical simulation, the curve of the dependence of the heating temperature of the fire-retardant steel column on the time of fire coincides with the experimental curves. It was found that the best convergence and,

accordingly, the smallest allowable deviation range have the dependences of the column temperature  $\theta_1$  with the temperatures that are calculated as a result of numerical simulations. Thus, the largest error in measuring temperatures is observed at 20 minutes of calculation and is 63°C. When comparing the results of numerical simulations with the results of tests for fire resistance of the fire-retardant column №2, such an error for 20 minutes was 92°C. It can be concluded that when using the results of tests for fire resistance of fire-retardant steel columns at the standard temperature of the fire, it is necessary to take the average value of the test results of two steel columns. Subsequently, the results of the average values of heating of two fire-retardant steel columns were used for comparison, as shown in Fig. 11.



**Fig. 11.** Dependence of the average temperature of fire-retardant steel columns №1 and №2 on the time of fire exposure according to the standard temperature of the fire: 1 – the experimental heating curve of columns №1 and №2; 2 – curve calculated as a result of numerical simulation

From Fig. 11 it follows that the experimental curve of the average temperature values of fire-retardant steel columns №1 and №2 and the curve calculated as a result of numerical simulation have a satisfactory convergence. The results of experimental studies and numerical analysis in the FRIEND program for a time interval of 20-40 minutes differ significantly in all control points, but later this difference is stabilized, and until the end of the experiment does not exceed 10.0%, which can be considered an acceptable result. All this indicates the correctness of setting the initial and boundary conditions, the construction of mathematical and physical models of thermal processes in the system “steel structure - fire-retardant coating”. Ultimately, proves the efficiency of the developed method for assessing the fire resistance of fire-resistant steel structures and the adequacy of real processes that occur when heating fire-resistant steel columns without applying a load under fire conditions at standard fire temperatures.

## 7 CONCLUSIONS

1. Geometric, physical, computer and finite element models for assessing the fire resistance of fire-resistant steel structures have been developed. The peculiarity of the developed models is taking into account the thermophysical characteristics of steel structures and fire-retardant coatings that depend on temperature, as well as taking into account the peculiarities of the formation of temperature regimes of fire.

2. Based on the offered models based on the developed calculation-experimental method of estimation of fire resistance of fire-resistant steel columns of I-section without the loading applied to them is estimated.

3. It is established that the best convergence and, accordingly, the smallest allowable deviation range have the dependences of the column temperature  $\theta_1$  with the temperatures

that are calculated as a result of numerical simulations. Thus, the largest error in measuring temperatures is observed at 20 minutes of calculation and is 63°C. When comparing the results of numerical simulations with the results of tests for fire resistance of the fire-retardant column №2, such an error for 20 minutes was 92°C. It is concluded that when using the results of tests for fire resistance of fire-retardant steel columns at the standard temperature of the fire, it is necessary to take the average value of the test results of two steel columns.

4. It is established that for the accuracy of fire resistance assessment of fire-resistant steel structures it is necessary to use the average values of temperatures of two fire-resistant steel columns. The best convergence of the results of experimental and calculated determination of the heating temperature of fire-retardant steel columns, which is not more than 10% of the allowable deviation. The efficiency of the proposed calculation and experimental method for assessing the fire resistance of fire-resistant steel structures and its adequacy to real processes in non-stationary heating of fire-resistant steel columns in the standard temperature of the fire.

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